

# C.U.SHAH UNIVERSITY

## Summer Examination-2017

Subject Name: Electromagnetics

Subject Code: 4TE06ELM1

Branch: B.Tech (EE,EEE)

Semester: 6

Date: 11/04/2017

Time: 02:30 To 05:30

Marks: 70

Instructions:

- (1) Use of Programmable calculator & any other electronic instrument is prohibited.
  - (2) Instructions written on main answer book are strictly to be obeyed.
  - (3) Draw neat diagrams and figures (if necessary) at right places.
  - (4) Assume suitable data if needed.
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Q-1

Attempt the following questions:

(14)

- 1) A unit vector has \_\_\_\_\_  
A) Only Direction B) Only Magnitude  
C) Both magnitude and direction D) None of the above
- 2) If A and B are the vectors, then  $A \times B = B \times A$   
A) True B) False
- 3) If  $\rho$  is a variable of Cylindrical co-ordinates, x and y are Cartesian co-ordinates, then \_\_\_\_\_  
A)  $\rho = x + y$  B)  $\rho = \sqrt{x^2 + y^2}$  C)  $\rho = x^2 + y^2$  D)  $\rho = x - y$
- 4) If A is a vector, then \_\_\_\_\_  
A)  $A \cdot A = 1$  B)  $A \cdot A = 0$  C)  $A \cdot A = A^2$  D)  $A \cdot A = A$
- 5) The gradient of a scalar V can be written as \_\_\_\_\_  
A)  $\nabla^2 V$  B)  $\nabla V$  C)  $\nabla \cdot V$  D)  $\nabla^2 V^2$
- 6) The divergence of vector A can be written as \_\_\_\_\_  
A)  $\nabla A^2$  B)  $\nabla^2 A$  C)  $\nabla \times A$  D)  $\nabla A$
- 7) For point P(-2, 6, 3), cylindrical co-ordinates are \_\_\_\_\_  
A) P (6.31, 108.43°, 3) B) P (7, 64.62°, 108.43°)  
C) (10, 90°, 75°) D) None of the above
- 8) Gauss Law is applicable to \_\_\_\_\_  
A) Open surface B) Open and Closed Surface  
C) Closed Surface D) None of the above



- 9) Laplace equation of a scalar  $V$  is given as \_\_\_\_\_  
 A)  $\nabla^2 V$  B)  $\nabla V$  C)  $-\nabla V$  D) None of the above
- 10) The equation for magnetic flux density is given by  $B =$  \_\_\_\_\_  
 A)  $\frac{H}{\mu^2}$  B)  $\frac{H}{\mu}$  C)  $\frac{\mu}{H}$  D)  $B = \mu H$
- 11) Points P and Q are located at P (10,2,4) and Q (-3,1,5) then distance between P and Q is \_\_\_\_\_  
 A) 13 B) 5.2 C) 0 D) 10
- 12) The relation between current density and electric field intensity is given by \_\_\_\_\_  
 A)  $J = \frac{\sigma}{E}$  B)  $J = \sigma E$  C)  $J = \frac{E}{\sigma}$  D)  $J = \sigma E^2$
- 13) For a cross product  $a_x \times a_y =$  \_\_\_\_\_  
 A)  $a_z$  B) 0 C)  $a_x$  D) 1
- 14) Curl of  $H =$  \_\_\_\_\_  
 A)  $\nabla H$  B)  $\nabla \times H$  C)  $\nabla^2 H$  D)  $\nabla H^2$

**Attempt any four questions from Q-2 to Q-8**

**Q-2 Attempt all questions (14)**

- (a) If  $\vec{A}$  is a vector, give the equation for vector  $\vec{A}$  in circular cylindrical coordinates. Give the relationship between Cartesian co-ordinates (x, y, z) and cylindrical co-ordinates ( $\rho, \phi, z$ ). **07**
- (b) Express the DEL ( $\nabla$ ) operator in Cartesian and Circular cylindrical co-ordinates. **07**

**Q-3 Attempt all questions (14)**

- (a) If  $Q_1$  and  $Q_2$  are the point charges are located at points having position vectors  $\vec{r}_1$  and  $\vec{r}_2$ , derive the equation of force  $\vec{F}_{12}$  on charge  $Q_2$  due to  $Q_1$ . **07**
- (b) Derive the equation for electric field intensity  $\vec{E}$  for a finite line charge with a uniform charge density  $\rho_L$ . **07**

**Q-4 Attempt all questions (14)**

- (a) Derive the equation for electric flux density  $\vec{D} = \frac{Q}{4\pi r^2} \vec{a}_r$ , where  $Q$  is the point charge. **07**



(b) Explain the divergence theorem. 07

**Q-5 Attempt all questions (14)**

(a) Derive the equation for magnetic field intensity with the help of Bio-Savart's law. 07

(b) Derive the equation of force  $\vec{F} = Id\vec{L} \times \vec{B}$ , where  $d\vec{L}$  = Length of differential element,  $\vec{B}$  = magnetic flux density,  $I$  = current through differential element 07

**Q-6 Attempt all questions (14)**

(a) Derive the equation of force  $\vec{F}_2 = \frac{\mu_0 I_1 I_2}{4\pi} \oint \left[ \frac{\vec{a}_{R_{12}} \times d\vec{L}_1}{R_{12}^2} \right] \times d\vec{L}_2$  between two 07

differential current elements. Where,

$\vec{F}_2$  = Force on element 2,  $d\vec{L}_1$  = Differential length of element 1

$d\vec{L}_2$  = Differential length of element 2,  $I_1$  = Current through element 1

$I_2$  = Current through element 2,  $R_{12}$  = Distance between element 1 and 2

(b) If  $\vec{A} = 10\vec{a}_x - 4\vec{a}_y + 6\vec{a}_z$ ,  $\vec{B} = 2\vec{a}_x + \vec{a}_y$ , Find 07

i) The component  $\vec{A}$  along  $\vec{a}_y$

ii) The magnitude of  $3\vec{A} - \vec{B}$

iii) A unit vector along  $\vec{A} + 2\vec{B}$

**Q-7 Attempt all questions (14)**

(a) For a co-axial cable at high frequencies, give the equation for capacitance, conductance, inductance and resistance. 07

(b) Find the gradient of the following scalar fields: 07

i)  $V = e^{-z} \sin 2x \cosh y$  ii)  $U = p^2 z \cos 2\phi$  iii)  $W = 10r \sin^2 \theta \cos \phi$

**Q-8 Attempt all questions (14)**

(a) Explain various types of antennas used for launching waves into space. 07

(b) Determine the divergence of the given vector fields. 07

i)  $P = x^2 y z \vec{a}_x + x z \vec{a}_z$  ii)  $Q = \rho \sin \phi \vec{a}_\rho + \rho^2 z \vec{a}_\phi + z \cos \phi \vec{a}_z$

